

EXISTENCE OF SOLUTIONS FOR AN ELLIPTIC PROBLEMS INVOLVING
 $p(x)$ –KIRCHHOFF-TYPE

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Abstract: In this paper, we show the existence of at least one non-trivial weak solutions to the nonlinear elliptic system with nonlocal term in \mathbb{R}^N : The main tool used is the variational method, more precisely, the Mountain Pass Theorem.

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